



Composite risers for deep waters using a numerical modelling approach

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ABSTRACT

There has been an increase in the application of composite structures in the oil and gas industry over the past four decades. This is due to more technological advancement and an increase in demand for the oil and gas. This trend has led to offshore exploration to transit from shallow water to deep water operations. Thus the need for more lightweight composite structures to reduce the deck loads and enable ease of operation. Composite risers are important as the properties of composite materials can be harnessed to improve riser performance and weight. This will enhance the development of deep water hydrocarbon reservoirs. In this paper, numerical stress analysis of composite offshore risers for deep water applications is carried out. ANSYS ACP is used for the finite element modelling of the composite riser for six load cases. From the design, recommendations for the design of the composite riser are made.

1. Introduction

The current demand for oil and gas has led to an increase in more technological advancements in the petroleum industry. This trend has resulted in offshore exploration to move from shallow waters to deep waters. This requires longer risers, resulting in significant weight increase. To improve riser performance, composite materials may be used. The composite materials offer advantages that can be harnessed within a riser design. The advantages include high corrosion resistance, fatigue resistance, high strength characteristics and increased weight savings. Thus, the composite structure becomes lightweight with low bending stiffness. Generally, marine risers are not independent structures, as they depend on other offshore structures like platforms and semisubmersibles [44,45]. The behaviour of composite risers in water, as offshore-dependent structures, are subject to environmental loads [3,19]. In order to design a composite riser, these loads must be carefully considered. Fig. 1 shows the typical structure of a composite riser, describing the different loads that act on it. A cross-section of the layers of the composite riser is also illustrated to show the composite make-up of the layers.

There has been significant interest in the potential deployment and utilisation of composite risers in deep water operations, particularly composite production risers (CPR). Thus, there is a need to use a novel

approach in investigating the stresses, deformations and buckling behaviour. Research on composite riser stems from studies on marine risers [56,16,7], composite tubes, composite cylinders, composite plates and shells [71,73,8,70,72]. Composite risers were first successfully deployed as a composite riser joint on the Heidrun Offshore Platform [52,13]. Further developments on composite riser designs have been made over the past three decades [67,42,47,4]. Previous research by joint industry presented the mechanical properties of composite tubes [60,57,55,51] and composite production risers for different design load cases [9,50,10,36]. Later, Doris Engineering presented a composite riser that introduced off-axis reinforcements at an angle of $\pm 55^\circ$ in order to reduce riser weight and improve efficiency [48]. In this study, netting theory was used. This assumes that the fibres in each layer are load-bearing, but that no stresses are present in the transverse direction. They concluded that the optimum angle for the design is $\pm 54.7^\circ$. This has led to advances in the modelling techniques like homogenization [58,59,12,2,61]. Advances relating to strength performance, debonding and delamination issues and riser components like the metal-composite interface (MCI) and end-fitting also exist in the literature [39,68,49,41,43]. Composite riser design concepts have been established by Airborne and Magma. Airborne developed thermoplastic composite pipes for offshore applications in deep waters [23,53,46]. Magma has developed the M-pipe, a composite pipe which can be used

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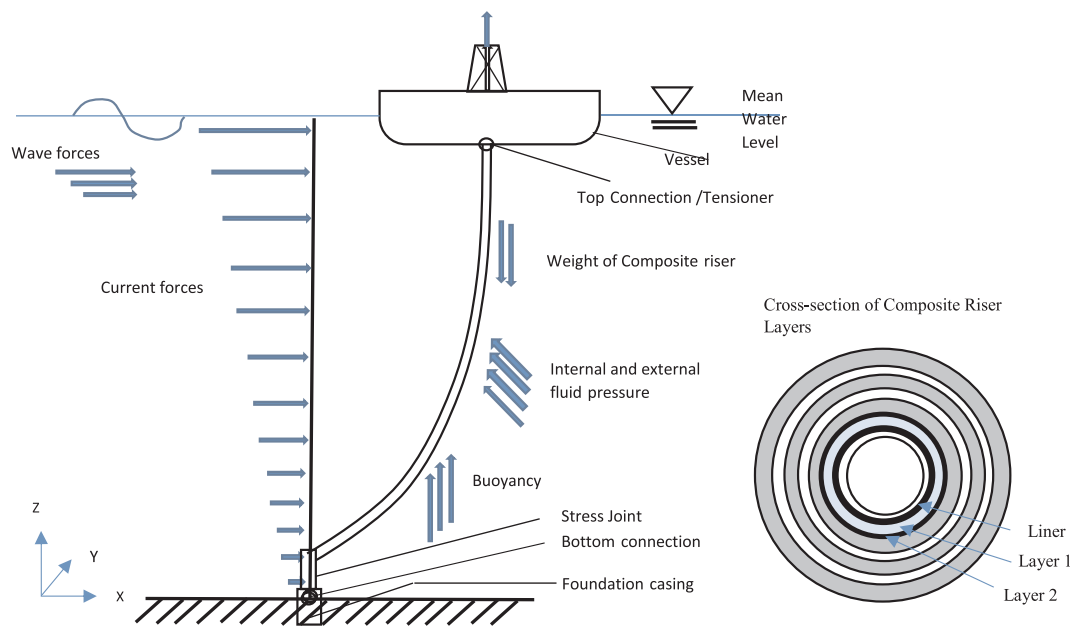


Fig. 1. Composite Riser System showing loads and cross-section of the layers.

in various applications [69,33]. According to Hatton [32], composite risers are an enabling technology, thus requiring qualification. Some qualification experience on composite riser are presented in literature [22,11,33,35]. However, qualification of deep water composite risers is still an issue in the industry. This necessitates the need to improve these designs through optimization [54,26,27]. Harte et al. [29,30] optimised a composite pipeline joint to reduce both the weight and peak stresses using a safety factor of 4.5. Fernandes da Silva et al. [25] presented another methodology for the optimization of composite risers using a Genetic Algorithm. Wang et al. [66] optimised a composite riser design using a surrogate-assisted evolutionary algorithm. The technique was applied to consider some critical load cases and thus reduce the structural weight. Manual tailoring of composite materials was carried out by using multiple variables to reduce the Finite Element Analysis (FEA). This resulted in a weight saving of 25% compared to the conventional method. Current optimized designs are presented in literature [34,63,66,62]. Some prototype designs of composite risers are also presented in some literature [5,15].

In this paper, composite riser design is presented for deployment in deep water applications by considering the maximum stress profile of the composite layers. The composite riser is designed for a 2000 m deep water application. The finite element model for the composite riser is developed with ANSYS ACP 19.0 [6]. In the local design, six (6) load cases are considered for the 3 m long CPR with 0.25 m inner diameter. The factor of safety profiles for the load cases are then presented in fibre, transverse and in-plane shear directions. An optimised design is presented using some design considerations. Six (6) different liner materials are investigated. The effect of tension during installation of the composite riser is also presented. In this study, a new approach is presented to obtain the stress in composite risers based on the strength of the composite materials used. The study will enhance the development of composite risers and support the deployment of composite risers and tubes in the offshore industry.

2. The design

2.1. Design approach

The design considered in this paper is for a 2000 m deep water riser using the parameters in Table 1. The tension calculation for the riser considers the effective weight of the riser based on the wall thickness

Table 1
Composite Riser Parameters.

Parameter	Value
Length of Riser (m)	3
Outer Diameter (m)	0.3048
Surface Area (m ²)	7.6605
Number of Layers	18
Water Depth (m)	2000

used. Three approaches are considered in the design of the composite riser: the analytical design, conventional design and the numerical design. The analytical design is used to derive the constitutive model for the composite riser. The conventional design is based on the orthogonal design of composites, where laminate reinforcements are arranged in only axial and hoop directions. In this method, the plies are in the orientations of 0° and 90°.

The reinforcements of the composite riser are designed in axial, angled and hoop directions. The mechanical properties of the composite materials considered are presented in Table 2. Different liner materials are also applied, as given in Tables 3. In addition, the stack-up sequence for the plies and the fibre orientations for the body of the composite riser are considered in the design, as given in Table 4. The design process starts with the design of the composite riser geometry in Design Modeler in ANSYS 19.0. Next, a Mechanical Model is developed in ANSYS Workbench. The Engineering Data are then developed and the model set up. It is then connected to the Static Structural model. Another setup using the same geometry with different liner thickness is developed. Next, an ACP (Pre) model is set-up and the material properties are developed. Then, the ACP (Post) model is also developed for the post-processing. The ACP (Pre) is then connected both the Static Structural model and the ACP (Post) model. Different design cases for the 6 loading conditions are considered. This process is carried out to get the best model for the design. The axial, off-axis and hoop reinforcements are all considered in the design procedure as presented. The initial design variables are first inputted. Next, the FEA is carried out using these values. The off-axis (angled) plies was determined as $\pm 53.5^\circ$ using Netting Theory [24,64,14,21,28]. However, the design was optimized as presented in Section 3.5. A maximum stress criterion is used to determine the layers/lamina that fail due to stresses exceeding the lamina strengths. This is used in calculating the Factor of

Table 2
Mechanical Properties of the unidirectional fibre-reinforced plastic composite.

Material	Density (kg/m ³)	E ₁ (GPa)	E ₂ = E ₃ (GPa)	G ₁₂ = G ₁₃ (GPa)	G ₂₃ (GPa)	σ_1^T (GPa)	σ_1^C (GPa)	σ_2^T (GPa)	σ_2^C (GPa)	τ_{12} (GPa)	$\nu_{12} = \nu_{13}$	ν_{23}
AS4/PEEK (APC2)	1561	131	8.7	5.0	2.78	1648	864	62.4	156.8	125.6	0.28	0.48
IM7/PEEK (APC2)	1320	172	8.3	5.5	2.8	2900	1300	48.3	152	68	0.27	0.48
P75/PEEK (APC2)	1773	280	6.7	3.43	1.87	668	364	24.8	136	68	0.30	0.69
AS4/Epoxy (938)	1530	135.4	9.37	4.96	3.2	1732	1256	49.4	167.2	71.2	0.32	0.46
P75/Epoxy (938)	1776	310	6.6	4.1	2.12	720	328	22.4	55.2	176	0.29	0.70
Glass fibre/Epoxy (S-2)	2464	87.93	16.0	9.0	2.81	4890	1586	55.0	148	70	0.26	0.28
Carbon fibre/Epoxy (T700)	1580	230	20.9	27.6	2.7	4900	1470	69	146	98	0.2	0.27

PEEK- Poly ether ether ketone; T700- Toray carbon fibre; S-2 – AGY glass fibre.

Subscript 1- fibre direction; subscript 2- transverse direction; subscript 3- in-plane shear direction.

Superscript T- tension; superscript C- compression.

Safety (F.S) for each of the layers.

2.2. Material properties

The parameters of the geometry were determined in the design stage as given in Table 1. Other important details include the thickness of the laminate layers, the stacking sequence, the liner thickness and the orientations of the fibre. High-performance materials are considered for both the fibre and matrix combinations. The reinforcement material considered for the fibres is high-strength AS4 carbon fibre. Two additional matrix materials that are considered in this study are the thermoplastic- PEEK, and the thermoset- Epoxy. The unidirectional lamina materials used in the Finite Element Analysis are PEEK composites. The PEEK material properties are used for the FEA analysis by considering the properties of the composite material. The properties for the Poisson's ratios (ν_1 , ν_2 and ν_3), the elastic moduli (E_1 , E_2 and E_3) and the shear moduli (G_{12} , G_{13} and G_{23}) are presented in Table 2. The subscripts 1 and 2 represent fibre and transverse directions, respectively. Subscript 12 represent the in-plane shear direction.

Generally, material properties of composites depend on conditions like the static loads, time, temperature, chemicals, water [37,38,72]. This affects the characteristic length of the composite structure. The material coordinate, also known as the rosette, is in XYZ coordinate system. Fig. 2 represents the global and material coordinate systems of the composite riser. Different layers have different material coordinates, and this was considered in the design in ANSYS ACP. In the global coordinate, the z-axis lies along the length of the composite riser, as shown in Fig. 2(a). The material coordinate, also known as the rosette, is in XYZ coordinate system. The material coordinate is relative to the fibre direction in x-axis, as shown in Fig. 2(b). The wall of the composite riser is considered a thick-walled pipe in the design and analysis. The materials are modelled by considering the mechanical behaviour of these materials. The composite riser also has in-plane effective properties and other material properties. Details of the material properties used in this investigation are presented in Tables 2 and 3. These data were extracted from technical sources [40,65,31,68].

Table 3
Mechanical Properties of the liner material.

Material	Density (kg/m ³)	Elastic Modulus (MPa)	Yield Stress (MPa)	Ultimate Stress (MPa)	Elongation at break (%)	Poisson's ratio, ν
Aluminium (1953T1)	2780	71	480	540	7.5	0.3
PA12	1010	540	1500	54	10	0.4
PEEK (Victrex)	1300	4.0	110	125	45	0.4
PVDF	1780	550	1540	54	10	0.4
Titanium (Ti6Al4V)	4430	113.8	880	950	14	0.342
Steel (X80)	7850	207	880	950	5.9	0.3

PA12- Polyamide 12; PEEK- Poly ether ether ketone; PVDF- Polyvinylidene fluoride.

Table 4
Stack-up Sequence and Orientation of Composite Plies.

Layer	Thickness (mm)	Orientation (°)	Description
0	2.0	0	Liner
1	1.58	0	Hoop Layers
2	1.58	0	
3	1.58	0	Off-axis Layers
4	1.58	0	
5	1.88	53.5	Off-axis Layers
6	1.88	−53.5	
7	1.88	53.5	Off-axis Layers
8	1.88	−53.5	
9	1.88	53.5	Off-axis Layers
10	1.88	−53.5	
11	1.88	53.5	Off-axis Layers
12	1.88	−53.5	
13	1.88	53.5	Off-axis Layers
14	1.88	−53.5	
15	1.62	90	Axial Layers
16	1.62	90	
17	1.62	90	
18	1.62	90	

2.3. Design load cases

The load that acts on a typical composite riser are as depicted in Fig. 1. In Table 5, six (6) different local design load cases are considered. The burst case (load case 1) is the critical load case and is therefore first investigated. The load cases implemented are recommended in industry standards on composite riser design [1,20,17,18]. The factor of 2.25 applied is according to test results as specified in ABS [1] as the ultimate tension strength of composite risers. The design load cases are carried out by considering the different stress components on the different fibre orientations. The stress distributions obtained based on these design load conditions are presented in Section 3.4.

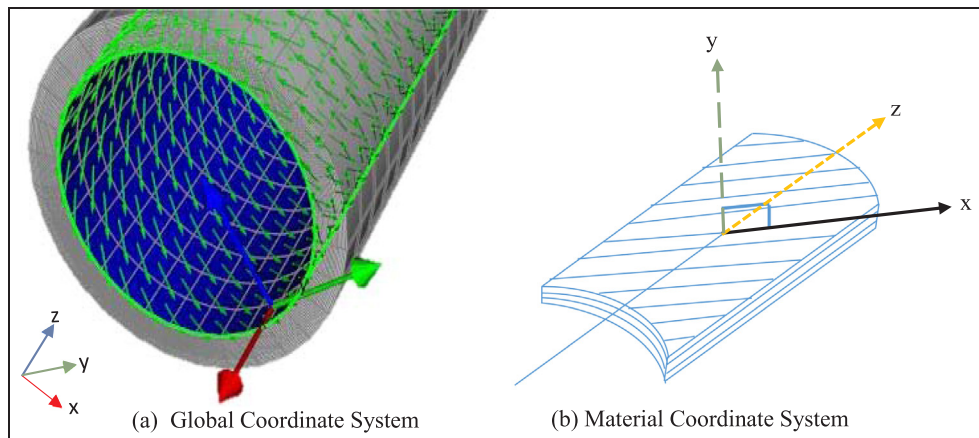


Fig. 2. The coordinate system for the composite riser showing the material rosette.

Table 5

Design Load Cases for Composite Riser.

Load Case	Name	Description
Load Case 1	Burst Case with end load effect	An internal pressure of 155.25 MPa is applied
Load Case 2	Collapse Case	An external pressure of 60 MPa is applied
Load Case 3	Pure Tension Case	The load factor of 2.25 with maximum tension
Load Case 4	Internal Pressure and Tension Case	An internal pressure of 155.25 MPa is applied on the tension
Load Case 5	External Pressure and Tension Case	The load factor of 2.25 is applied on 19.5 MPa external pressure
Load Case 6	Buckling Case	An external pressure of 60 MPa is applied

Table 6

Mesh Study used in Finite Element Analysis.

Mesh Cases	Axial Divisions	Circumferential Divisions	Number of Nodes	Number of Elements	Stress in Fibre Direction (2nd layer at 0°)	Stress in Transverse Direction (1st layer at 0°)	Stress in Transverse Direction (14th layer at 0°)	Stress in In-plane Shear Direction (7th layer at 0°)
1	30	80	16,950	2400	39.8865	20.8857	29.584	38.9907
2	40	80	22,600	3200	40.2943	20.9098	29.654	38.9572
3	50	80	28,250	4000	40.483	20.9209	29.6862	38.9416
4	60	80	33,900	4800	40.5853	20.9269	29.7037	38.933
5	80	80	45,200	6400	40.6873	20.9328	29.7211	38.9245
6	100	80	56,500	8000	40.7345	20.9356	29.7291	38.9206
7	120	80	67,800	9600	40.7602	20.9371	29.7334	38.9185

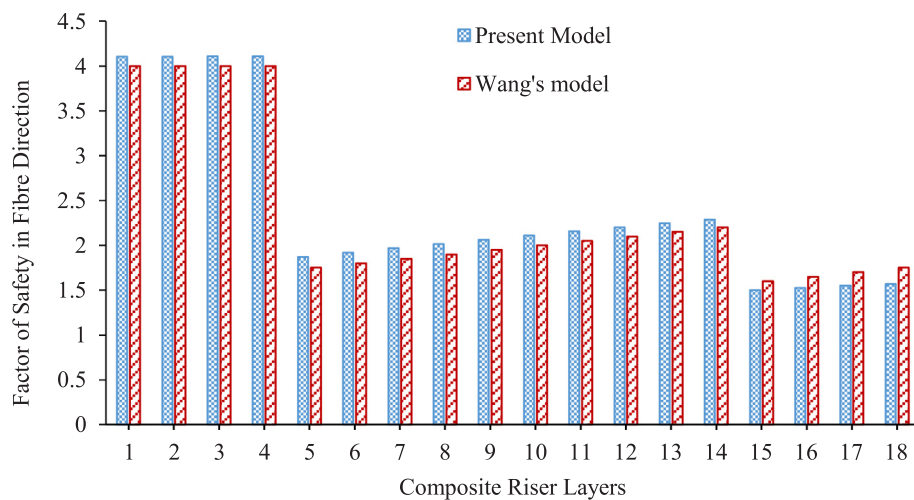


Fig. 3. Validation of Model with Wang's model under Burst Case in fibre direction for AS4/Epoxy with Aluminium liner using a factor of safety of composite layers reinforced using $[0_4, (\pm 53.5)_5, 0_4]$ configuration.

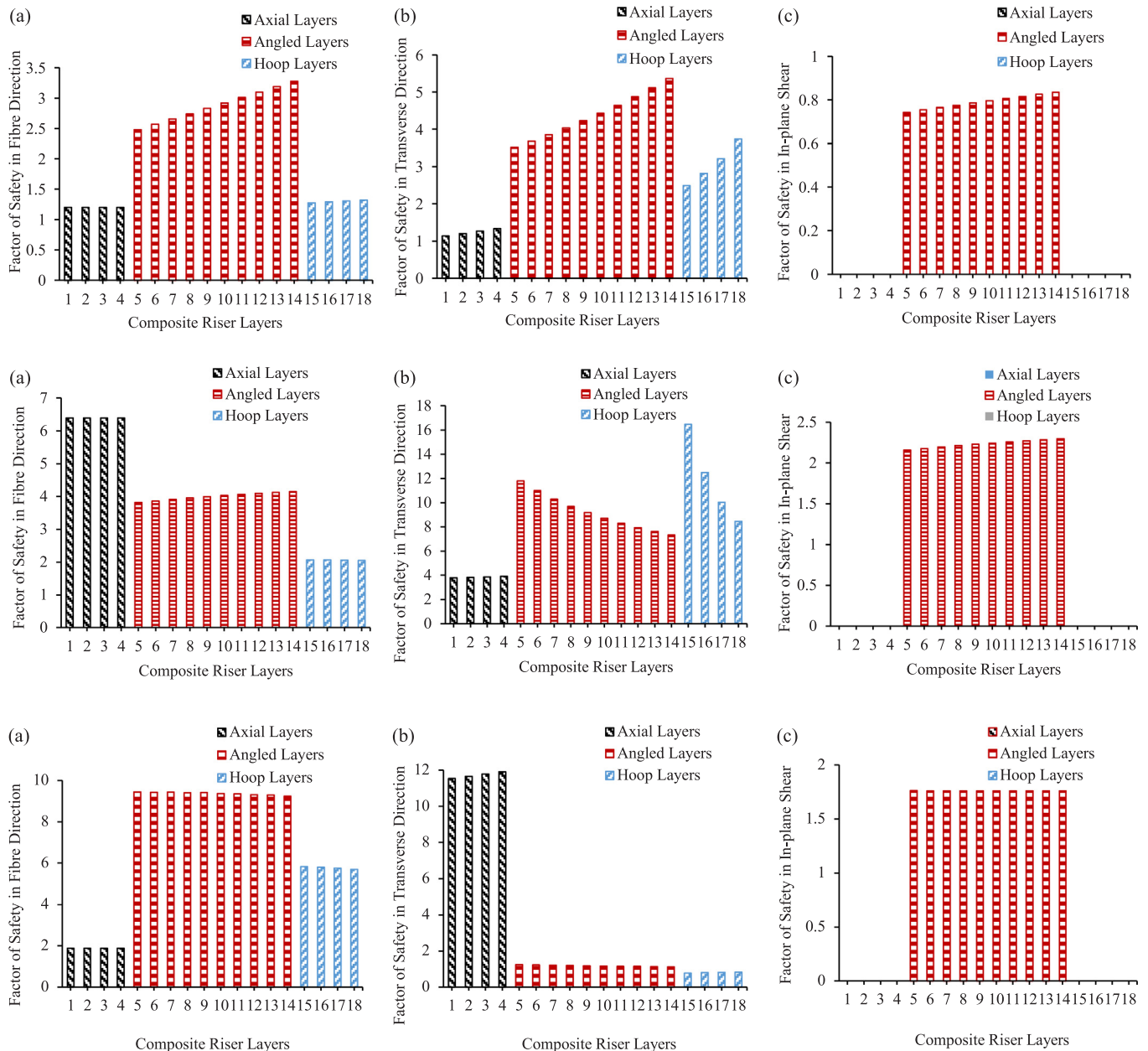


Fig. 4. Factor of Safety profiles for the layers of the composite riser using AS4/Epoxy and titanium liner with $[0_4, (\pm 53.5)_5, 90_4]$ configuration under: i) burst load case in (a) Fibre Direction, (b) Transverse Direction, (c) In-plane Shear Direction; ii) collapse load case in (a) Fibre Direction, (b) Transverse Direction, (c) In-plane Shear Direction; and iii) pure tension load case in (a) Fibre Direction, (b) Transverse Direction, (c) In-plane Shear Direction.

3. Numerical model

3.1. Finite element model

The Finite Element (FE) model of the 3 m composite riser is developed in ANSYS ACP. The parameters for the composite riser is given in Table 1. The fixed end boundary condition is considered at both ends to represent the closed pipe during operation and test conditions as given in ABS standard [11]. Solid 186 elements are used as 3D layered structural solid elements. This type of element supports quadratic displacements and also exhibits translation motion in three degrees of freedom about its 20 nodes. Solid 186-layered elements are deployed in simulating the laminates of the composite riser, whereas Solid 186-homogenous elements are used for simulating single elements like the liners in the radial direction. The solver applies the thickness of the element using the nodal coordinates. This assists in modelling the stack-up of

the laminates and the modelling plies. Thus, the complete layup is developed in the defined material coordinate called the rosette. The methodology for the local design involved using the load cases to obtain stress values for each composite layer for different thicknesses. Details on some theories on the stresses are available in literature [72,74]. The first step in the finite element analysis is to predict the riser behaviour, with some initial values estimated for the composite layers. The burst case is carried out with a 155.25 MPa internal pressure by considering the boundary condition at the fixed end supports. This represents the actual test scenario for testing composite risers, composite tubes and composite pipes for offshore applications. The stresses were obtained from selected element location on the composite riser.

In the FEA, a quadrilateral mesh type is applied. The FEA model is designed with 30 axial divisions and 80 circumferential divisions, involving 16,950 nodes and 2400 elements. The composite riser is analysed as a shell body in ANSYS ACP 19.0. Multiple material layup

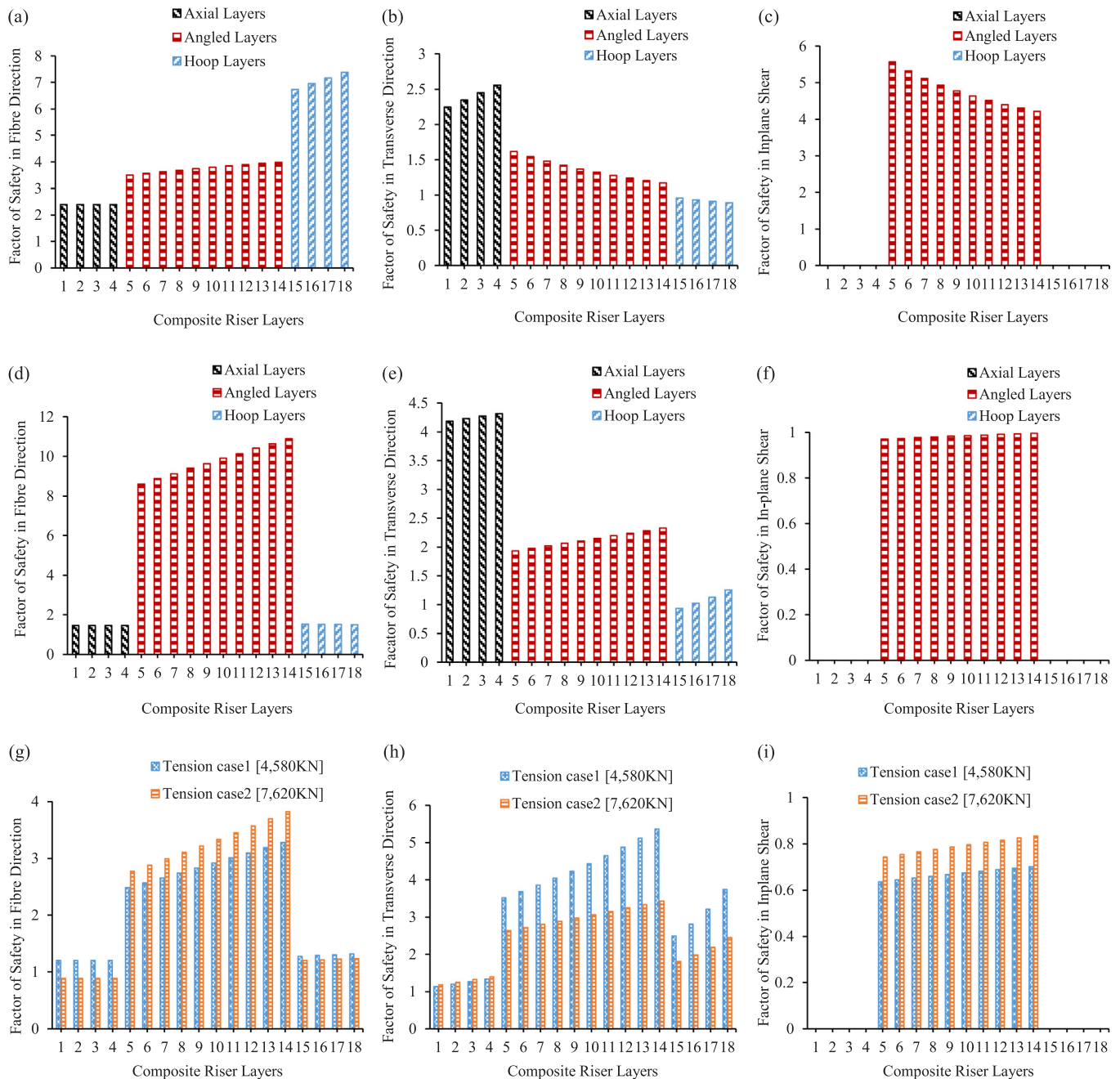


Fig. 5. Factor of Safety profiles for the layers of the composite riser configured with AS4/Epoxy and $[0_4, (\pm 53.5)_5, 90_4]$ configuration under: i) tension with internal pressure load case using titanium liner in (a) Fibre Direction, (b) Transverse Direction, (c) In-plane Shear Direction; ii) tension with external pressure load case using titanium liner in (d) Fibre Direction, (e) Transverse Direction, (f) In-plane Shear Direction; and iii) burst load case with end load effect using aluminium liner to investigate the effect of tension force during installation in (g) Fibre Direction, (h) Transverse Direction, (i) In-plane Shear Direction.

configurations are designed with 18 layers considered in each CPR design. Different liner materials are used in conducting the analysis for each case study. In this design, the axis for the layers for the material as designed from outer layer to inner layer, is shown in Fig. 2(a). The finite element model showing the stack-up for the materials for the composite riser with $[0_4, (\pm 53.5)_5, 90_4]$ configuration in ANSYS ACP (Pre) is as illustrated in Table 4.

3.2. Convergence study

The finite element model of the composite body includes meshing. A convergence study is carried out using the mesh of the composite riser model, as presented in Table 6. The convergence study is estimated

using the maximum values of the maximum total deformation. The objective is to determine the best mesh size for the numerical analysis of the composite riser to save computation time. The mesh convergence study represents the number of elements against the stress components for the fibres from the inner wall (liner). From the results, the mesh size in mesh case 1 was used in the study. It was selected considering the stress profiles for the selected stress components, as presented in Table 6.

3.3. Validation

The results obtained for the local design of the composite riser are validated using the results obtained from the model by Wang et al. [67]

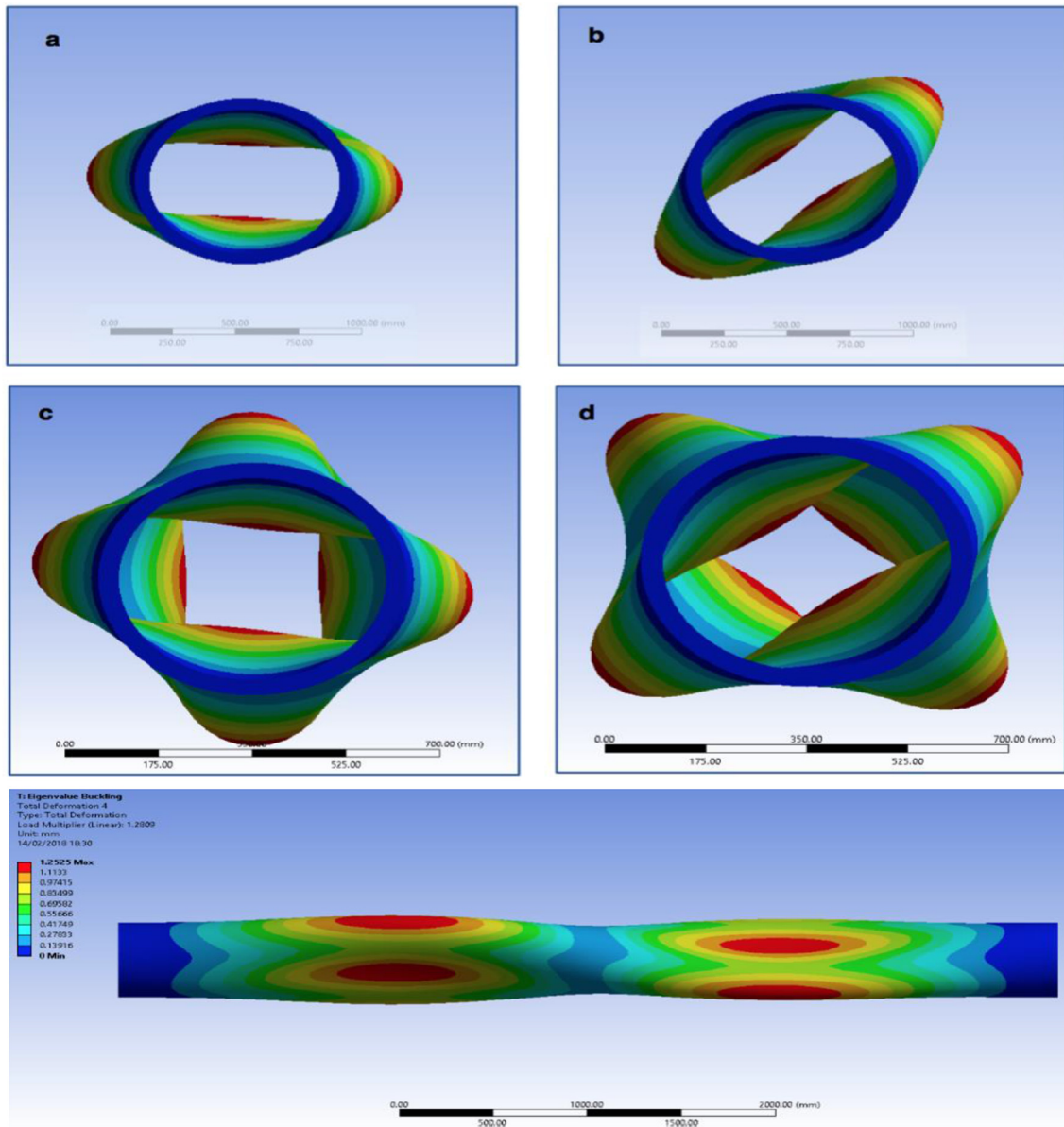


Fig. 6. Eigenvalue Buckling Analysis showing end view of modes 1–4 deformation (a–d) and the plan view of mode 4 deformation (e), in ANSYS 19.0, relatively scaled for visualization.

Table 7

Results of the Eigenvalue buckling analysis.

Results of Eigenvalue Buckling Analysis				
Mode	1	2	3	4
Buckling Pressure (MPa)	75.6	75.6	76.8	76.8
Number of Axial Half-Waves	1	1	2	2
Number of Circumferential Waves	2	2	2	2
Maximum Deformation (mm)	1.00	1.33	1.00	1.25

as presented in Fig. 3. This model was developed for the numerical stress analysis of composite risers using 3D elements. Compared to the present model, the factor of safety is higher than the factor of safety in Wang's model. This is due to the difference in homogenization method applied in Wang's model and different mesh divisions - 150 divisions in axial direction and 80 divisions in circumferential direction. However, there is a pattern in the stress distribution on both models. Wang's model was subjected to internal pressure and end effect for the burst

case. However, there is a pattern in the stress distribution on both models. In the axial layers (layers 1–4), the factor of safety in the present model decreases from 3.25 to 2.35, whereas in Wang's model, the decrease is from 4.00 to 3.80. In the angled layers (layers 5–14), the factor of safety increases from 1.90 to 3.60, whereas in Wang's model, the increase is from 1.80 to 2.20. In the hoop layers (layers 15–18), the factor of safety in the present model increases from 1.36 to 1.40, whereas in Wang's model, the increase is from 1.60 to 1.70. The variance for the axial, angled and hoop layers are about 0.8, 0.4 and 0.2 respectively. This confirms the accuracy of the results for the present model. In addition, the similarity in the axial, angled and hoop layers is also an indication of the validity of the present model.

3.4. Result analysis and discussion

Fig. 4(a–i) and 5(a–f) are the results for the design loads for the composite riser as presented in Section 2.3. The composite structure was modelled in ANSYS ACP using a 3D-element as presented in Section 3.1. Results are obtained for the stress components in the fibre,

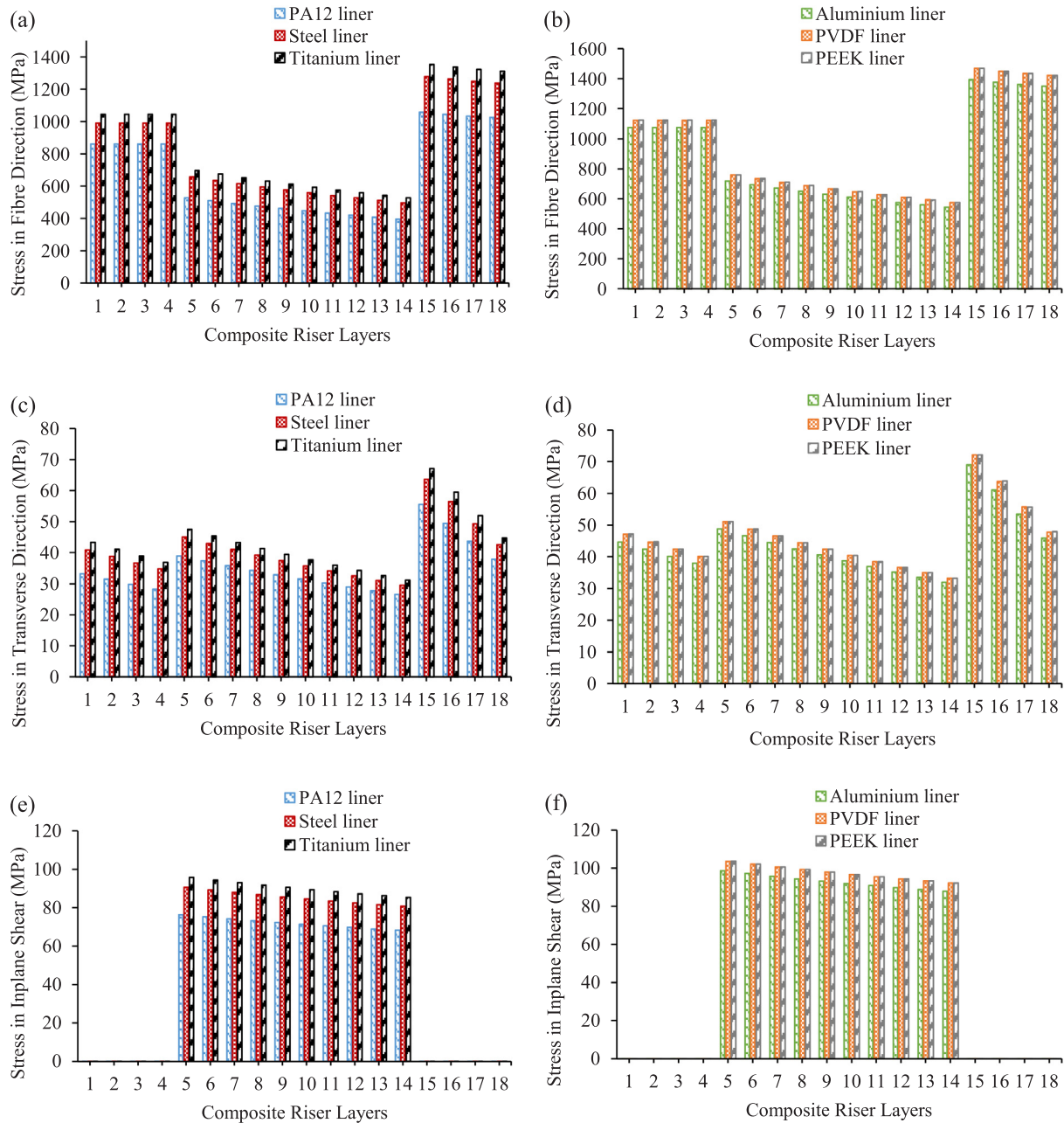


Fig. 7. Stress profiles of composite riser design configured using AS4/Epoxy in $[0_4, (\pm 53.5)_5, 90_4]$ to investigate the effect of different liner materials in the Fibre Direction (a, b); the transverse direction (c, d); and the in-plane shear direction (e, f).

transverse and in-plane shear directions. As these results were below the minimum safety factor of 1, the design satisfied the requirements as detailed in the ABS standard [1]. The design must be optimised in order to have composite riser structure with better performance as presented in Section 3.5. The Factor of Safety was then obtained using the strength values in Table 2 and Eq. (1);

$$\text{Factor of Safety (F.S.)} = \frac{\text{Allowable Strength}}{\text{Actual Strength}} \quad (1)$$

Fig. 4(a–c) shows the results for the burst load; Fig. 4(d–f) shows the results for the collapse load; Fig. 4(g–i) shows the results for the pure tension load; Fig. 5(a–c) shows the results for the tension with internal pressure load while Fig. 5(d–f) shows the results for the tension with external pressure load. The composite riser is designed using AS4/Epoxy and 2 mm thick titanium liner is applied with $[0_4, (\pm 53.5)_5, 90_4]$ configuration. An internal pressure of 155.25 MPa is applied in the

burst case with end effect. For the collapse case, an external pressure of 60 MPa is applied. This design cases determine the performance of the layers. However, the ability of each layer to withstand the internal pressure is also dependent on the liner. The burst load case with end effect was first carried out to determine the thickness of the composite riser. It also shows the critical performance characteristics of the composite riser.

In Fig. 5(g–i), the effect of tension force on the fibres during installation is also investigated. Two tension cases were used: 4580 kN and 7620 kN loads are applied in tension case 1 and case 2 respectively. The investigation is carried out for a composite riser of 18 layers. Burst load was applied using AS4/Epoxy and Aluminium liner with $[0_4, (\pm 53.5)_5, 90_4]$ configuration. As is observed in Fig. 5(g–i), an increase in the tension force decreases the Factor of Safety in the axial layers and hoop layers but increases the Factor of Safety in the off-axis layers. This means that, as the tension increases, the stresses on the axial and hoop

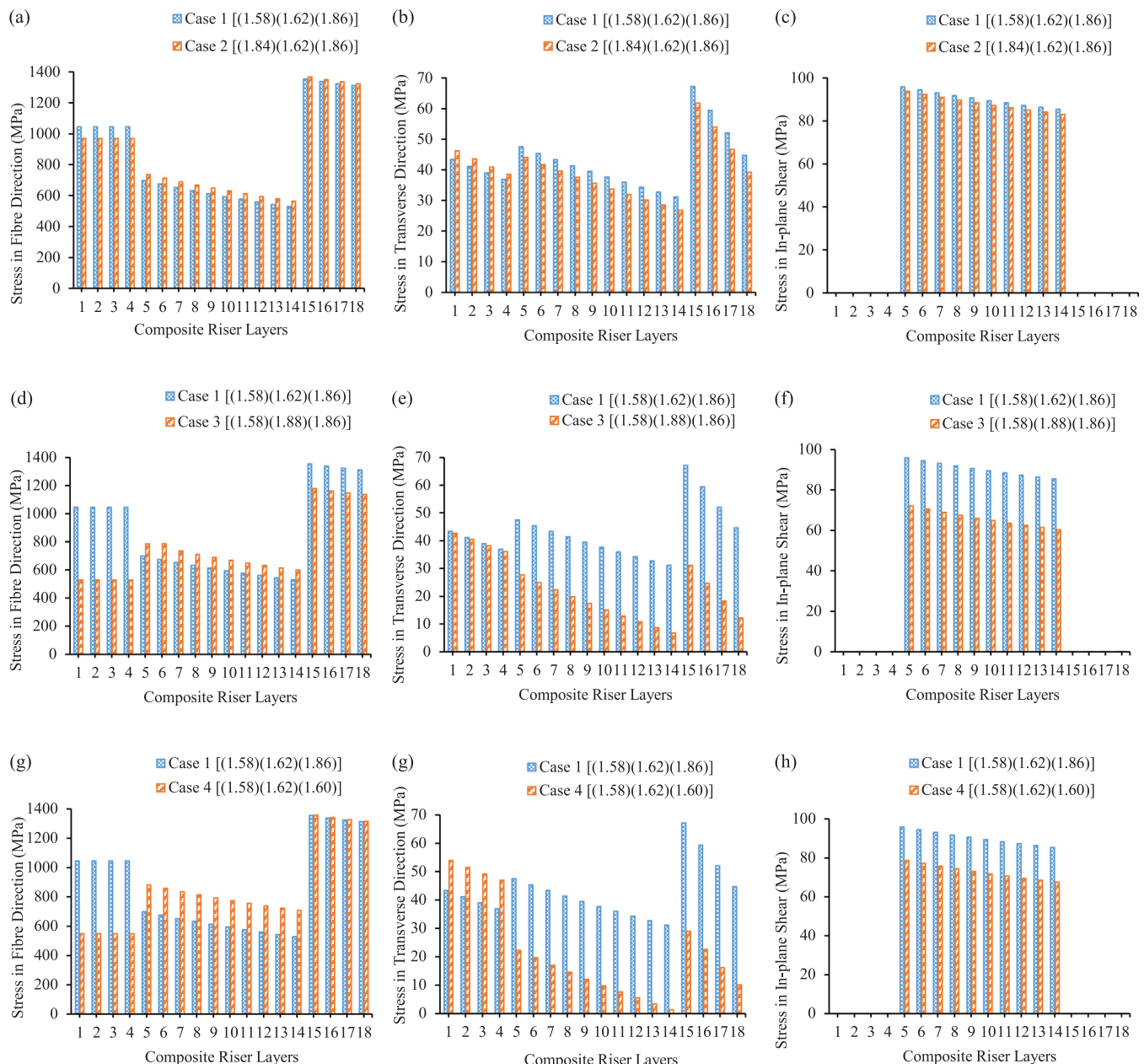


Fig. 8. AS4/Epoxy and Aluminium liner with $[0_4(\pm 53.5)_5, 90_4]$ configuration of composite riser on the effect of: i) the axial layer thickness in the (a) Fibre Direction, (b) Transverse Direction, (c) In-plane Shear Direction; ii) the off-axis layer thickness in the (d) Fibre Direction, (e) Transverse Direction, (f) In-plane Shear Direction; iii) and the hoop layer thickness in the (g) Fibre Direction, (h) Transverse Direction, and (i) In-plane Shear Direction.

layers increase while the stresses decrease at the off-axis layers. The tension ratio for both cases investigated is 1:1.7. Considering the fibre direction, the axial layers had a 25.8% decrease in the Factor of Safety. In the off-axis layers, there is an 11.7% increase in the Factor of Safety. In the hoop layers, there is a 5% decrease in the Factor of Safety. This means that, the off-axis is properly reinforced to carry the tension force in the fibre direction. Looking at the transverse direction, the axial layers had a 4.4% increase in the Factor of Safety. In the off-axis, there is 25% decrease in the Factor of Safety. In the hoop axis, there is 27.3% decrease in the Factor of Safety. From these, we can conclude that an increase in the tension force will increase the stresses in the off-axis and hoop layers, implying a decrease in their Factors of Safety, respectively. Considering the In-plane shear direction, the Factors of Safety in both the axial and the hoop layers are infinity as they are negligible but not exactly zero, as shown in Fig. 5(c, f, i). In the off-axis layers, there is a 16.8% increase in the Factor of Safety. Thus an increase in tension will

decrease the stresses in the off-axis layers in the in-plane shear direction.

In Fig. 6(a–e), different modes on the buckling analysis carried out on the CPR design are presented. An external pressure of 60 MPa is applied using linear buckling analysis. Fig. 6(a–d) is the end view for different mode shapes for modes 1–4 while Fig. 6(e) shows a plan view of mode 4. Mode 1 has the most critical buckling effect for the CPR design [28]. Table 7 presents the maximum deformations, axial waves and circumferential waves obtained. From the results, Modes 1 and 2 have the critical buckling pressure of 75.6 MPa is approximately 30% higher than the design buckling pressure of 60 MPa. It is noteworthy that the mode shapes are not shown in true scale of the deformation but with a relative scale factor for visualization.

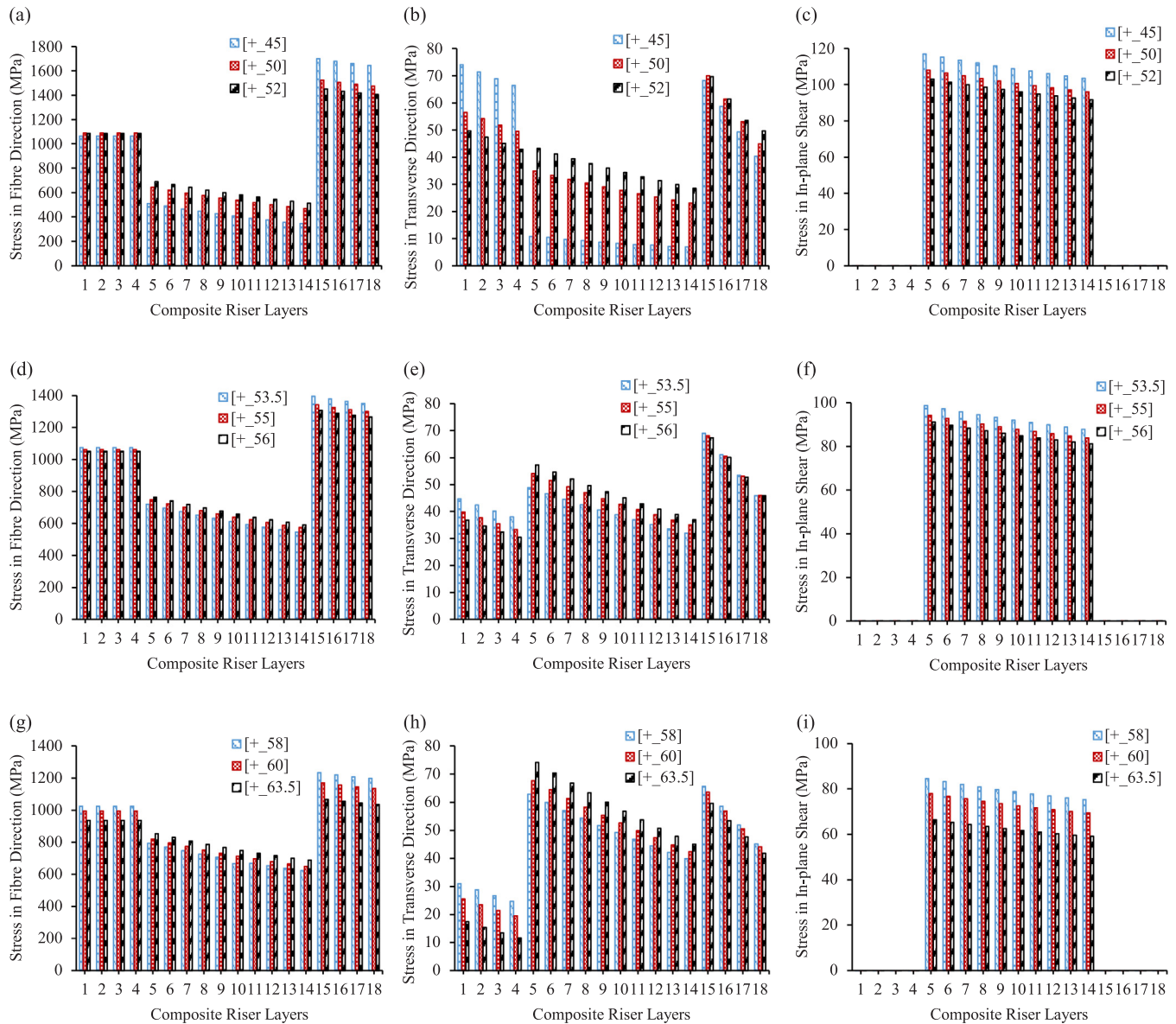


Fig. 9. Stress profiles for composite riser configured using AS4/Epoxy and Aluminium liner to investigate off-axis layer orientation on: i) $[0_4, (\pm 45)_5, 90_4]$, $[0_4, (\pm 50)_5, 90_4]$, $[0_4, (\pm 52)_5, 90_4]$ in: (a) Fibre Direction, (b) Transverse Direction, (c) In-plane Shear Direction; ii) $[0_4, (\pm 53.5)_5, 90_4]$, $[0_4, (\pm 55)_5, 90_4]$, $[0_4, (\pm 56)_5, 90_4]$ in: (d) Fibre Direction, (e) Transverse Direction, (f) In-plane Shear Direction; and iii) $[0_4, (\pm 58)_5, 90_4]$, $[0_4, (\pm 60)_5, 90_4]$, $[0_4, (\pm 63.5)_5, 90_4]$ in: (g) Fibre Direction, (h) Transverse Direction, and (i) In-plane Shear Direction.

3.5. Optimisation

The results obtained from the design load cases in Section 3.4 were further analysed to obtain an optimal design. Different design concepts were considered in this section. The purpose of the optimisation is to reduce the material utilised, reduce the weight of the composite riser and also ensure that the strength of the composite riser can withstand the different design load cases. To optimise the composite riser design, some considerations for the optimisation are presented in Sections 3.5.1–3.5.5. The parameters considered are the thickness of the fibre layers, thickness of the hoop layers, thickness of the off-axis layers, type of liner material, thickness of liner material, type of composite material, the number of layers, and the orientation of the layers.

3.5.1. Consideration 1: Different liner materials

Fig. 7(a–f) represents the stress distribution for the effect of liners on the AS4/Epoxy composite riser designed using $[0_4, (\pm 53.5)_5, 90_4]$ configuration. The effect of different liner materials is investigated on

six (6) different liner materials: PA12, steel, Titanium, Aluminium, PVDF and PEEK liners are analysed. The same liner thickness of 2 mm and layer thickness ratio of 1.58:1.62:1.86 were applied for all the cases. For the analysis, PA12 liner had the least stress values in all the stress components. This means, that newer liner designs can be carried out using the PA12 material, as this also has good liner properties for composite riser applications, as seen in Fig. 7(a). Steel liner performed better than titanium liner. In Fig. 7(b), the PEEK liner and the PVDF liner were approximately the same stress, with the maximum stress value of 1450.99 MPa at the hoop layers in fibre direction.

3.5.2. Consideration 2: Layer thickness

Fig. 8(a–c) represents the stress distribution for the effect of axial layer thickness on AS4/Epoxy composite riser with Aluminium liner. Two cases were compared with same configuration $[0_4, (\pm 53.5)_5, 90_4]$ but layer thickness ratio of 1.58:1.62:1.86 and 1.64:1.62:1.86 respectively. The compared cases show that the higher the axial layer thickness, the less the stress distribution in the axial layers in the fibre

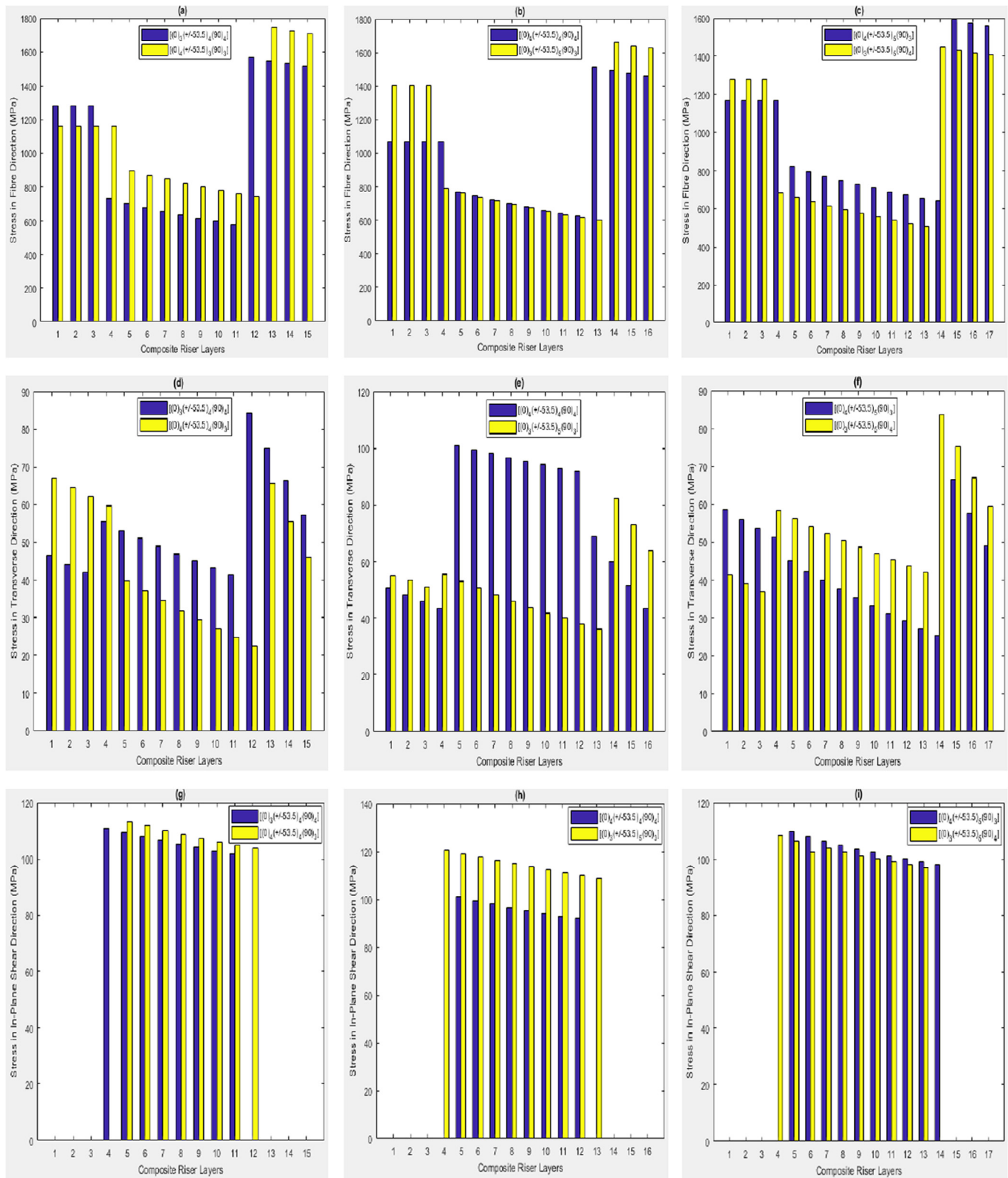


Fig. 10. Stress profiles for the layers of AS4/Epoxy Composite Riser design with aluminium liner applied in optimization consideration (5) to investigate the effect of the number of layers in the fibre direction (a, b, c); the transverse direction (d, e, f) and the In-plane Shear Direction (g, h, i) on $[0_3(\pm 53.5)_4, 90_4]$, $[0_4(\pm 53.5)_3, 90_3]$, $[0_4(\pm 53.5)_4, 90_4]$, $[0_3(\pm 53.5)_5, 90_3]$, $[0_4(\pm 53.5)_5, 90_3]$ and $[0_3(\pm 53.5)_5, 90_4]$.

direction. However, this increases the stresses in the off-axis layers and the hoop layers. Thus, the axial layers will withstand more stresses in the fibre direction than in the other layers in the same stress component. This is due to the alignment of the fibres in the 0° angle being

axially laid along the composite riser body. In the transverse direction, an increase in the thickness of the axial layer will increase the stress in axial layers but decrease the stresses in the off-axis layers and hoop layers. In the in-plane shear direction, an increase in the axial layer

Table 8
Summary of benefits of the optimisation.

Optimisation	Impact on the Design
Decrease axial laminae orientation	There is noticeable reduction in the tensile stresses in fibre direction under the pure tension load case. The axial fibres have an increase in the stresses in the in-plane shear component.
Decrease hoop laminae orientation	There is noticeable reduction in the tensile stresses in fibre direction. The hoop fibres have an increase in the stresses in the in-plane shear component.
Increase off-axis laminae orientation	There is redistribution of stress. The equivalent stress in the liner decreases. Maximum stress in the fibre direction in both the hoop and axial layers slightly change in non-critical off-axis laminae.
Increase axial layer thickness	Reduction in the equivalent stress in the liner. Reduction in the maximum stress in the fibre direction of the hoop layers. Maximum stress in the transverse direction of the axial layers decrease.
Increase hoop layer thickness	Reduction in the equivalent stress in the liner. Maximum stress in the fibre direction of the hoop layers decrease. Maximum stress in the transverse direction of the axial layers decrease.
Iteratively decrease liner and hoop laminae thickness	The equivalent stress in the liner increases to a value slightly below the allowable stress of the aluminium liner. There is an increase in the maximum stresses in both the fibre direction and transverse direction to within 97% and 99% of the corresponding allowable stresses, respectively.

thickness decreases the stress in the off-axis layers.

Fig. 8(d–f) represents the stress distribution for the effect of off-axis layer thickness using AS4/Epoxy with Aluminium liner with same configuration $[0_4, (\pm 53.5)_5, 90_4]$. Two cases were analysed of layer thickness ratio 1.58:1.62:1.86 and 1.58:1.88:1.86 respectively. The compared cases show that the higher the off-axis or angled layer thickness, the less the stress distribution in the axial layers and the hoop layers in the fibre direction. However, this increases the stresses in the off-axis layers. Thus, the off-axis layers will withstand more stresses in the fibre direction than in the other layers in the same stress component. In the transverse direction, an increase in the thickness of the off-axis layer will decrease the stress in all the layers. In the in-plane shear direction, an increase in the off-axis layer thickness decreases the stress in the off-axis layers.

Fig. 8(g–i) represents the stress distribution for the effect of hoop layer thickness using AS4/Epoxy with Aluminium liner with same configuration $[0_4, (\pm 53.5)_5, 90_4]$. Two cases were analysed of layer thickness ratio 1.58:1.62:1.86 and 1.58:1.62:1.60 respectively. The compared cases show that the higher the hoop layer thickness, the higher the stress distribution in the axial layers in the fibre direction. However, this decreases the stresses in both the off-axis layers and the hoop layers. Thus, the hoop layers will withstand more stresses in the fibre direction than when the thickness is increased but not much, compared to other layers. Also, an increase in the thickness of the hoop layers in the transverse direction will decrease the stress in the axial layers but increase the stresses in both the off-axis layers and the hoop layers. In the in-plane shear direction, an increase in the hoop layer thickness increases the stress in the off-axis layers.

3.5.3. Consideration 3: Different composite materials

Different composite materials were also applied for the same configuration to ascertain the best performance using $[0_4, (\pm 53.5)_5, 90_4]$ as the composite riser design configuration. They are AS4/PEEK (APC2), IM7/PEEK (APC2), P75/PEEK (APC2), AS4/Epoxy (938), P75/Epoxy (938), Glass fibre/Epoxy (S-2) and Carbon fibre/Epoxy (T700). The mechanical properties of these composite materials are presented in Table 2. From the analysis, the best performance chosen was AS4/Epoxy (938), based on material weight and strength.

3.5.4. Consideration 4: Layer orientations

Fig. 9(a–f) represents the stress distribution for the effect of off-axis layer orientation using AS4/Epoxy with Aluminium liner for different configurations. The following off-axis angles were investigated: $\pm 45^\circ$, $\pm 50^\circ$, $\pm 52^\circ$, $\pm 53.5^\circ$, $\pm 55^\circ$, $\pm 56^\circ$, $\pm 58^\circ$, $\pm 60^\circ$, and $\pm 63.5^\circ$. From the results, the best performance was observed in $\pm 63.5^\circ$. This was considered the best angle for the optimum design. Also, the orientations of other layers were also investigated. The stress distribution for the effect of axial layer orientation and hoop layer orientation were also investigated. An increase in the fibre layer angle from 0° increase the

stresses in the fibre, transverse and in-plane shear stress components. In the in-plane shear, the stress values in the axial layers also increases from zero. This implies that the strength property in the in-plane shear can be affected by an increase in the orientation of the fibre layers. Different orientations were investigated, such as $[(0)_4, (\pm 53.5)_5, (90)_4]$, $[(0)_4, (\pm 53.5)_5, (89)_4]$ and $[(0)_4, (\pm 53.5)_5, (88)_4]$. The results show that a decrease in the hoop layer angle from 90° increases the stresses in the fibre, transverse and in-plane shear stress components. In the in-plane shear, the stress values in the hoop layers increases from zero. This implies that the strength property in the in-plane shear can be altered by increasing the orientation of the hoop layers slightly.

3.5.5. Consideration 5: Number of layers

Different designs were analysed during the optimization of the composite riser layers. In Fig. 10(a–i), six configurations are presented under burst load case. They are $[0_3, (\pm 53.5)_4, 90_4]$, $[0_4, (\pm 53.5)_3, 90_3]$, $[0_4, (\pm 53.5)_4, 90_4]$, $[0_3, (\pm 53.5)_5, 90_3]$, $[0_4, (\pm 53.5)_5, 90_3]$ and $[0_3, (\pm 53.5)_5, 90_4]$ design configurations. They were compared with the $[0_4, (\pm 53.5)_5, 90_4]$ design presented on Fig. 4(a–c). The $[0_4, (\pm 53.5)_5, 90_4]$ design performed better among the cases analysed for the number of layers. However, the results from Fig. 10 showed that an increase in the number of layers will reduce the stresses on the layers.

3.5.6. Optimised design

An optimised design was obtained based on the considerations given in Sections 3.5.1–3.5.5. The design configuration $[0_4, (\pm 63.5)_5, 90_4]$ is the optimised design selected. An increase in the off-axis ply orientation reduced the stresses in the critical load case. Fig. 9 shows different designs considered as using $\pm 63.5^\circ$ produced the least marginal stress profiles. Minimizing the thickness of the liner and hoop laminae was also considered. Thus, the thickness of the optimal design is 1.58:1.62:1.60. Table 8 gives a summary of the benefits of the optimisation process and its impact on the design.

4. Conclusion

The numerical study of the composite riser was successfully designed using the given material properties. Six design load cases were carried out to ascertain the stresses on the composite riser wall. The local design has been successfully carried out on a 3 m composite riser for deep water applications. The composite riser lay-up has 18 layers excluding the liner. The same configuration $[0_4, (\pm 53.5)_5, 90_4]$, liner thickness of 2 mm and layer thickness ratio of 1.58:1.62:1.86 was considered in the local design. Overall, the methodology for this design presented safe design. The Factor of Safety for the composite risers for different load cases is presented to guide offshore designers on composite risers. From the designs, the thickness of the layers helped to reduce the stresses on the layers. For all the design load cases, the burst

case was considered the most crucial as it had the highest stress effect on the layers. Thus, it determined the design configuration and is important in ascertaining the structural performance of composite risers. For the burst case, the hoop layers in the fibre direction had more stress distributions. This stress effect is due to the resultant force directions acting along the layers of the riser. From this local design, $[0_4, (\pm 63.5)_5, 90_4]$ and thickness ratio 1.58:1.62:1.60 is the optimised design selected. The design had the best resistance to burst load compared to the other designs analysed. Five different considerations were applied in the optimization as depicted in Figs. 7–10. From the parametric optimization, the best design was selected based on the different stress components. The study showed that the liner absorbed some pressure during the burst case. However, it is necessary to optimize the design with external liners but there is no need to reinforce the inner liners further. This implies that the optimised composite riser design will have high strength and withstand harsh environmental conditions. However, further research is recommended on the global analysis of the composite riser for deep ocean conditions, and the vortex-induced effect.

Conflict of interest

There is no conflict of interest on this research work.

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Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.compstruct.2018.11.057>.

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